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ABSTRACT. [11446] Prove or disprove: There exist 2×2 symmetric integer matrices A and B such that for all words $w(X, Y), u(X, Y)$ in letters $\{X, Y\}$, we have $w(A, B) = u(A, B)$ if and only if $w = u$.

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