

**Connections for Women: Joint Workshop on
Commutative Algebra and Cluster Algebras**

August 22, 2012 to August 24, 2012

MSRI, Berkeley, CA, USA

Organizers:

Claudia Polini (University of Notre Dame)

Idun Reiten (Norwegian University of Science and Technology)

Karen Smith (University of Michigan)

Lauren Williams* (University of California, Berkeley)

Final Report for the MSRI Connections for Women Workshop: Commutative algebra and cluster algebras

Organizers: Claudia Polini, Idun Reiten, Karen Smith, and Lauren Williams

The goal of this workshop was to give an introduction to topics in commutative algebra and cluster algebras, via talks and a mini-course, all of which were given by women. (However, the audience was a mix of men and women.) A secondary goal was to encourage and facilitate the exchange of ideas between researchers in commutative algebra and researchers in cluster algebras. The workshop consisted of:

1. **A mini-course** on the topic of cluster algebras, together with a problem session.
2. **Nine lectures**, some of which were expository, and some of which were research talks.
3. **A poster session**, in which junior researchers presented their results.
4. **A panel discussion**, in which several tenure-track and tenured female professors discussed issues related to being a female mathematician.

In addition to these activities, there were multiple tea breaks, and a wine and cheese social, in which participants could get to know each other and discuss mathematics.

Details on the minicourse and lectures

Minicourse on cluster algebras

Lauren Williams gave two lectures which introduced the notion of cluster algebra, and gave several examples, including the coordinate ring of the Grassmannian. She gave several problems for participants to think about, and Kelli Talaska led a problem session to help participants with these problems.

Lectures on commutative algebra

Claudia Miller (Professor of Mathematics at Syracuse University) spoke on 'Duality for Koszul Homology over Gorenstein Rings'. She first explained the classical results, due to Herzog, and then reported on recent developments obtained in collaboration with Hamid Rahmati and Janet Striuli. The aim of their work is to show that the duality forces the Cohen-Macaulayness of the Koszul homology modules whenever a certain amount of local depth is present. Irena Swanson (Professor of Mathematics at Reed College) talked about 'Minimal components over certain binomial ideals'. The work done in collaboration with Amelia Taylor, Julia Porcino, and Alessio Sammartano, spanned three different papers. Their original goal was to understand Alex Fink's paper on minimal components arising in algebraic statistics. In several instances they express the minimal components in terms of some combinatorial structures. Vijaylaxmi Trivedi (Professor at Tata Institute of Fundamental Research, Mumbai, India) delivered a lecture on her recent work on Hilbert-Kunz multiplicities. The Hilbert-Kunz multiplicity is a fundamental invariant that like the ordinary multiplicity carries meaningful information about the singularities of a local Noetherian

ring in characteristic p . The Hilbert-Kunz multiplicity has been instrumental to prove, for instance, that tight closure does not localize. Unlike the ordinary multiplicity, the Hilbert-Kunz multiplicity is very difficult to compute and any result that sheds light on this mysterious invariant is a great progress towards the understanding of the structure of rings in positive characteristic. Maria Evelina Rossi (Professor of Mathematics at the University of Genova, Italy) presented recent results concerning isomorphism classes of Artin K -algebras through Macaulay's inverse system. The goal was to prove that the study of certain classes of Artin local rings can be reduced to the study of standard graded K -algebras. Interesting application to the rationality of the Poincaré series were given. Finally, Alicia Dickenstein (Professor of Mathematics at the University of Buenos Aires, Argentina) described the use of linear syzygies for the implicitization of rational surfaces. These algebraic techniques, based on the theory of approximation complexes due to Jürgen Herzog, Aron Simis and Wolmer Vasconcelos, were introduced in this setting by Laurent Bus, Marc Chardin and Jean Pierre Jouanolou, whose work was inspired by the "practical" method of moving curves, proposed by Thomas Sederberg and Falai Chen.

Lectures on cluster algebras

There were four lectures on topics related to cluster algebras. Karin Baur gave a talk on *Cluster algebras, quiver mutation, and triangulations*, which was an expository talk on cluster algebras associated to surfaces. The combinatorics of such cluster algebras is encoded by triangulations of the surface. Gordana Todorov gave an expository talk on *Relations between cluster algebras and cluster categories*, in which she explained how the *cluster category* provides a categorification of a cluster algebra. In this construction, cluster variables are replaced by quiver representations, and one may use the representation theory of quivers to understand the corresponding cluster algebra. Konstanze Rietsch gave a talk on *Mirror symmetry for Grassmannians*, in which she explained how to construct the superpotential by using the cluster algebra structure on Grassmannians. Kelli Talaska gave a talk on *Networks and the Deodhar decomposition of real Grassmannians*, which explained how to parameterize Deodhar components in the Grassmannian. (This construction generalizes Postnikov's parameterization of cells in the totally non-negative part of the Grassmannian.)

Conclusion

We were extremely pleased with the outcome of the MSRI Connections workshop on commutative algebra and cluster algebras, and think that it was a very rewarding experience for the participants.

Participants seemed to enjoy the minicourse and lectures very much, and there were a number of questions after each talk. The atmosphere during the conference was very friendly and down-to-earth. One person wrote "I am very happy to say I never expected such an incredible experience getting to meet so many wonderful people from staff to students to mathematician." Other participants commented that they enjoyed being at a conference with so many women. The panel discussion was a lively discussion that involved both men and women in the audience. The men seemed to find the discussion very interesting, and one senior male mathematician asked what male mathematicians can do to help female mathematicians.

Organizers

| First Name | Last Name | Institution |
|------------|-----------|--|
| Claudia | Polini | University of Notre Dame |
| Idun | Reiten | Norwegian University of Science and Technology |
| Karen | Smith | University of Michigan |
| Lauren | Williams | University of California (Lead Organizer) |

Speakers

| First Name | Last Name | Institution |
|---------------|-------------|--|
| Karin | Baur | Karl-Franzens-Universität Graz |
| Alicia | Dickenstein | University of Buenos Aires |
| Claudia | Miller | Syracuse University |
| Konstanze | Rietsch | King's College London |
| Maria Evelina | Rossi | Università di Genova |
| Irena | Swanson | Reed College |
| Kelli | Talaska | University of California |
| Gordana | Todorov | Northeastern University |
| Vijaylaxmi | Trivedi | Tata Institute of Fundamental Research |
| Lauren | Williams | University of California |



**Connections for Women:
Joint Workshop on Commutative Algebra and Cluster Algebras
August 22 - 24, 2012**

Schedule

| Wednesday, August 22, 2012 | | | |
|-----------------------------------|-------------------|---------------------|--|
| 9:00 AM - 9:15 AM | Simons Auditorium | | Welcome |
| 9:15 AM - 10:15 AM | Simons Auditorium | Lauren William | Mini Course: Basics of Cluster Algebras |
| 10:15 AM - 10:45 AM | Atrium | | Coffee Break |
| 10:45 AM - 11:35 AM | Simons Auditorium | Claudia Miller | Duality for Koszul Homology over Gorenstein Rings |
| 11:35 AM - 12:30 PM | Atrium | | Poster Session I |
| 12:30 PM - 2:00 PM | Atrium | | Lunch |
| 2:00 PM - 2:50 PM | Simons Auditorium | Karin Baur | Cluster algebras, quiver mutation and triangulations. |
| 2:50 PM - 3:30 PM | Atrium | | Poster Session II |
| 3:30 PM - 5:00 PM | Atrium | | Wine and cheese social |
| Thursday, August 23, 2012 | | | |
| 9:00 AM - 10:00 AM | Simons Auditorium | Lauren Williams | Mini Course: Basics of Cluster Algebras |
| 10:00 AM - 10:30 AM | Atrium | | Coffee Break |
| 10:30 AM - 12:00 PM | Simons Auditorium | Kelli Talaska | Discussion session for the Mini Course |
| 12:00 PM - 1:30 PM | Atrium | | Lunch |
| 1:30 PM - 2:20 PM | Simons Auditorium | Irena Swanson | Minimal components over certain binomial ideals |
| 2:30 PM - 3:20 PM | Simons Auditorium | Vijaylaxmi Trivedi | Hilbert-Kunz multiplicity and Hilbert-Kunz slope |
| 3:30 PM - 4:00 PM | Atrium | | Tea break |
| 4:00 PM - 4:50 PM | Simons Auditorium | Gordana Todorov | Relations between Cluster Algebras and Cluster Categories. |
| Friday, August 24, 2012 | | | |
| 9:00 AM - 10:00 AM | Simons Auditorium | Konstanze Rietsch | On mirror symmetry for Grassmannians |
| 10:00 AM - 10:30 AM | Atrium | | Coffee Break |
| 10:30 AM - 11:20 AM | Simons Auditorium | Maria Evelina Rossi | Analytic Isomorphisms of Artin local $\mathbb{K}\langle S \rangle$ -algebras |
| 11:30 AM - 12:20 PM | Simons Auditorium | Kelli Talaska | Networks and the Deodhar decomposition of real Grassmannians |
| 12:30 PM - 2:00 PM | Atrium | | Lunch |
| 2:00 PM - 2:50 PM | Simons Auditorium | Alicia Dickenstein | Implicitization techniques: easy algorithms, deep proofs. |
| 3:00 PM - 3:30 PM | Atrium | | Tea break |
| 3:30 PM - 5:00 PM | Simons Auditorium | | Panel Discussion |

| Participants | | |
|---------------------|------------------|---|
| First Name | Last Name | Institution |
| Kathleen | Ansaldi | University of Notre Dame |
| Federico | Ardila | San Francisco State University |
| Spencer | Backman | Georgia Institute of Technology |
| Helene | Barcelo | MSRI - Mathematical Sciences Research Institute |
| Emily | Barnard | North Carolina State University |
| Karin | Baur | Karl-Franzens-Universität Graz |
| Arkady | Berenstein | University of Oregon |
| Christine | Berkesch Zamaere | Duke University |
| Florian | Block | UC Berkeley Math Faculty |
| Mats | Boij | Royal Institute of Technology (KTH) |
| Sarah | Brodsky | University of California |
| Man-Wai | Cheung | University of California, San Diego |
| Steven | Collazos | San Francisco State University |
| Aldo | Conca | Università di Genova |
| Alicia | Dickenstein | University of Buenos Aires |
| Idan | Eisner | University of Haifa |
| Sabine | El Khoury | American University of Beirut |
| Laura | Escobar | Cornell University |
| Sara | Faridi | Dalhousie University |
| Anna | Felikson | Jacobs University Bremen |
| Xiao | Feng | Michigan State University |
| Alex | Fink | North Carolina State University |
| Bruce | Fontaine | MSRI - Mathematical Sciences Research Institute |
| Claudio | Fontanari | Università degli Studi di Trento |
| Louiza | Fouli | New Mexico State University |
| Alexander | Garver | University of Minnesota Twin Cities |
| Michael | Gekhtman | University of Notre Dame |
| Sira | Gratz | Universität Hannover |
| Elizabeth | Gross | University of Illinois |
| Emily | Gunawan | University of Minnesota Twin Cities |
| Ines | Henriques | University of California |
| Daniel | Hernandez | University of Minnesota Twin Cities |
| Olga | Holtz | University of California |
| Aline | Hosry | Notre Dame University, Lebanon |
| Alina | Iacob | Georgia Southern University |
| Srikanth | Iyengar | University of Nebraska |
| Jack | Jeffries | University of Utah |
| haridas | kalbhor | University of Pune, Maharashtra (India) |
| Adam | Kalman | University of California |
| Steven | Karp | UC Berkeley Math Faculty |
| Leila | Khatami | Union College--Union University |
| Robert | Korsan | retired |
| Kaie | Kubjas | Freie Universität Berlin |
| Manoj | Kummini | Chennai Mathematical Institute |
| Volha | Kushel | TU Berlin |
| Lisa | Lamberti | Eidgenössische TH Zürich-Zentrum |
| Phillpp | Lampe | Universität Bielefeld |
| Kuei-Nuan | Lin | University of California |
| Jichun | Liu | Zhejiang University |
| Antonio | Macchia | Università di Bari |
| Diane | Maclagan | University of Warwick |

| | | |
|---------------|-----------------|---|
| Jeff | Madsen | University of Notre Dame |
| Paolo | Mantero | Purdue University |
| Robert | Marsh | University of Leeds |
| Sarah | Mayes | University of Michigan |
| Jason | McCullough | MSRI - Mathematical Sciences Research Institute |
| Claudia | Miller | Syracuse University |
| Jonathan | Montano | Purdue University |
| Sophie | Morier-Genoud | Université de Paris VI (Pierre et Marie Curie) |
| Gregg | Musiker | University of Minnesota Twin Cities |
| Leatitia | Mutombo | University Of Kinshasa |
| Alfredo | Nájera Chávez | Université de Paris VII (Denis Diderot) |
| Tomoki | Nakanishi | Nagoya University |
| BHARATH | NARAYANAN | Pennsylvania State University |
| Alyssa | Palfreyman | San Francisco State University |
| Rebecca | Patrias | University of Minnesota Twin Cities |
| Servando | Pineda Carranza | San Francisco State University |
| Pierre-Guy | Plamondon | Université de Caen |
| Claudia | Polini | University of Notre Dame |
| Fan | QIN | Université de Paris VII (Denis Diderot) |
| Jenna | Rajchgot | MSRI - Mathematical Sciences Research Institute |
| Denise | Rangel | University of Texas |
| idun | reiten | Norwegian University of Science and Technology |
| Vladimir | Retakh | Rutgers University |
| Konstanze | Rietsch | King's College London |
| Elina | Robeva | University of California |
| Maria Evelina | Rossi | Università di Genova |
| dylan | rupel | MSRI - Mathematical Sciences Research Institute |
| Steven | Sam | University of California |
| Jennifer | Schaefer | Dickinson College |
| Gus | Schrader | UC Berkeley Math Faculty |
| Alexandra | Seceleanu | University of Nebraska |
| Anurag | Singh | University of Utah |
| Karen | Smith | University of Michigan |
| Suresh | Srinivasamurthy | Kansas State University |
| Janet | Striuli | Fairfield University |
| Irena | Swanson | Reed College |
| Kaisa | Taipale | MSRI - Mathematical Sciences Research Institute |
| Kelli | Talaska | University of California |
| Geetha | Thangavelu | Institute of Mathematical Sciences |
| Howard | Thompson | University of Michigan |
| Gordana | Todorov | Northeastern University |
| vijaylaxmi | trivedi | Tata Institute of Fundamental Research |
| Bernd | Ulrich | Purdue University |
| Alexander | Vainshtein | University of Haifa |
| Yadira | Valdivieso Diaz | Universidad Nacional de Mar del Plata |
| Emanuele | Ventura | Università di Catania |
| Roger | Wiegand | University of Nebraska |
| Sylvia | Wiegand | University of Nebraska |
| Lauren | Williams | University of California |
| Emily | Witt | University of Minnesota Twin Cities |
| Nora | Youngs | University of Nebraska |
| Josephine | Yu | Georgia Institute of Technology |
| Andrei | Zelevinsky | Northeastern University |

Officially Registered Participant Information

| | | |
|---------------------|--|------------|
| Participants | | 104 |
|---------------------|--|------------|

| | | |
|--------------------------|--------|------------|
| Gender | | 104 |
| Male | 46.15% | 48 |
| Female | 53.85% | 56 |
| Declined to state | 0.00% | 0 |

| | | |
|--------------------------|--------|------------|
| Ethnicity* | | 104 |
| White | 65.38% | 68 |
| Asian | 14.42% | 15 |
| Hispanic | 8.65% | 9 |
| Pacific Islander | 0.00% | 0 |
| Black | 1.92% | 2 |
| Native American | 0.00% | 0 |
| Mixed | 0.96% | 1 |
| Declined to state | 8.65% | 9 |

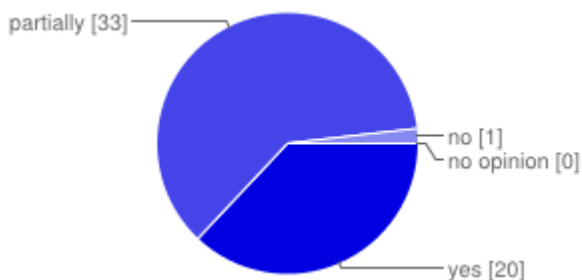
* ethnicity specifications are not exclusive

54 [responses](#)

Summary [See complete responses](#)

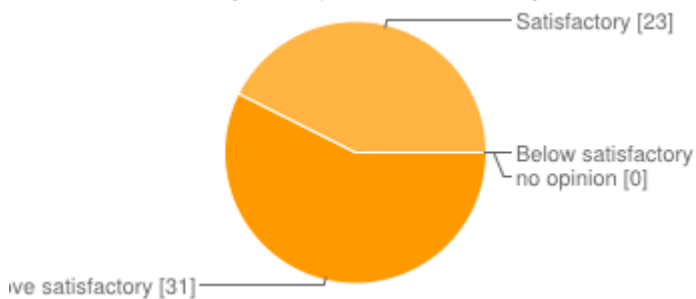
Topic presentation and organization

Did the various topics within the workshop integrate into a coherent picture?



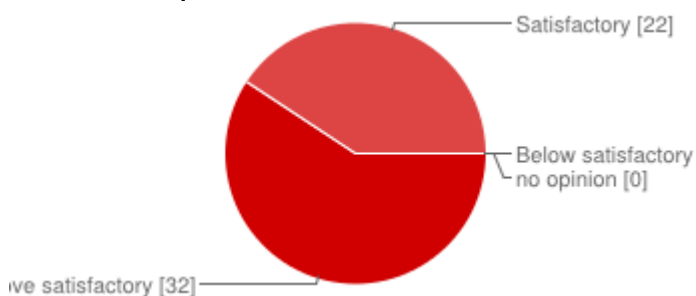
| | | |
|------------|----|-----|
| yes | 20 | 37% |
| partially | 33 | 61% |
| no | 1 | 2% |
| no opinion | 0 | 0% |

Were the speakers generally clear and well organized in their presentation?



| | | |
|--------------------|----|-----|
| Above satisfactory | 31 | 57% |
| Satisfactory | 23 | 43% |
| Below satisfactory | 0 | 0% |
| no opinion | 0 | 0% |

Was there adequate time between lectures for discussion?



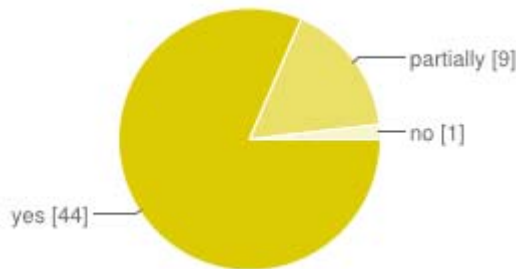
| | | |
|--------------------|----|-----|
| Above satisfactory | 32 | 59% |
| Satisfactory | 22 | 41% |
| Below satisfactory | 0 | 0% |
| no opinion | 0 | 0% |

Additional comments on the topic presentation and organization

It is wonderful the second talk on the first day was more of a research talk than an introductory talk With the exception of the minicourse the talks were extremely specialized. Perhaps speakers shou ...

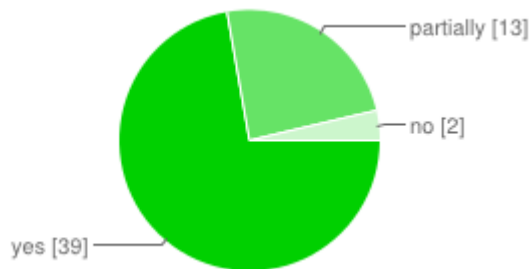
Personal assessment

Was your background adequate to access a reasonable portion of the material?



| | | |
|-----------|-----------|-----|
| yes | 44 | 81% |
| partially | 9 | 17% |
| no | 1 | 2% |

Did the workshop increase your interest in the subject?



| | | |
|-----------|-----------|-----|
| yes | 39 | 72% |
| partially | 13 | 24% |
| no | 2 | 4% |

Was the workshop worth your time and effort?



| | | |
|-----------|-----------|-----|
| yes | 52 | 96% |
| partially | 1 | 2% |
| no | 1 | 2% |

Additional comments on your personal assessment

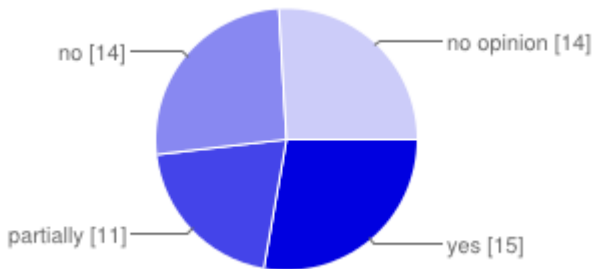
The lectures on Cluster Algebras were more accessible than the ones in Commutative Algebra.

The latter were directed mainly to specialists, it seems; a pity.

The talks really help me to understand m ...

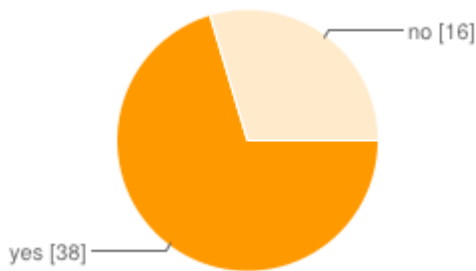
Additional Activities

Did you find the poster sessions beneficial?



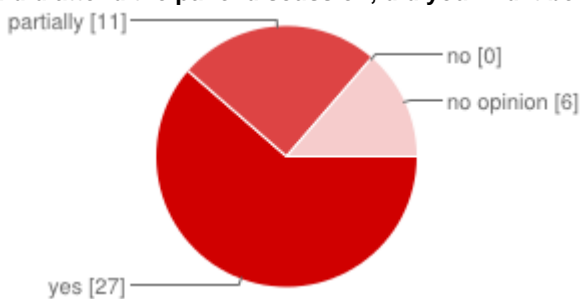
| | | |
|------------|-----------|-----|
| yes | 15 | 28% |
| partially | 11 | 20% |
| no | 14 | 26% |
| no opinion | 14 | 26% |

Did you attend the panel discussion?



| | | |
|-----|-----------|-----|
| yes | 38 | 70% |
| no | 16 | 30% |

If you did attend the panel discussion, did you find it beneficial?



| | | |
|------------|-----------|-----|
| yes | 27 | 50% |
| partially | 11 | 20% |
| no | 0 | 0% |
| no opinion | 6 | 11% |

Connections for Women: Joint Workshop on Commutative Algebra and Cluster Algebras, August 22 to 24, 2012 at MSRI, Berkeley, CA USA

What other subjects should be addressed in future panel discussions?

Hold the panel discussion earlier - it

stimulates discussion.

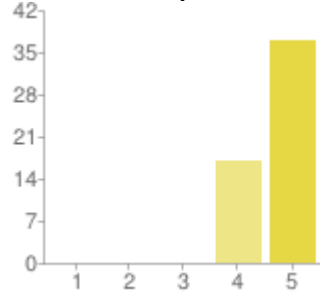
Probably it's best just to let things flow freely. This worked here and it

should work in the future.

If it is important for faculty to k ...

Venue

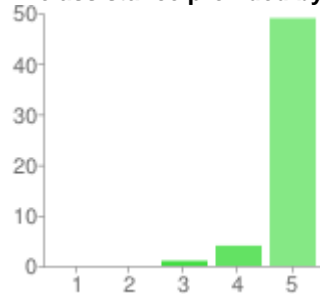
Your overall experience at MSRI



| | | |
|-----------------------|-----------|-----|
| 1 -Not satisfactory | 0 | 0% |
| 2 | 0 | 0% |
| 3 | 0 | 0% |
| 4 | 17 | 31% |
| 5 -Above satisfactory | 37 | 69% |

Not satisfactory Above satisfactory

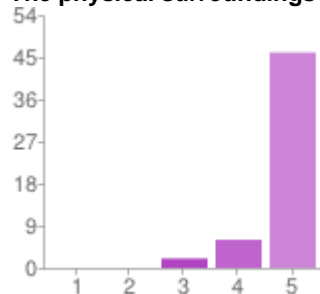
The assistance provided by MSRI staff



| | | |
|-----------------------|-----------|-----|
| 1 -Not satisfactory | 0 | 0% |
| 2 | 0 | 0% |
| 3 | 1 | 2% |
| 4 | 4 | 7% |
| 5 -Above satisfactory | 49 | 91% |

Not satisfactory Above satisfactory

The physical surroundings

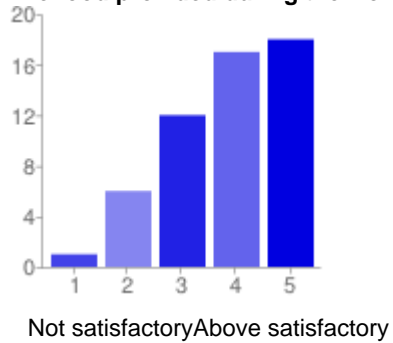


| | | |
|-----------------------|-----------|-----|
| 1 -Not satisfactory | 0 | 0% |
| 2 | 0 | 0% |
| 3 | 2 | 4% |
| 4 | 6 | 11% |
| 5 -Above satisfactory | 46 | 85% |

Not satisfactory Above satisfactory

Connections for Women: Joint Workshop on Commutative Algebra and Cluster Algebras, August 22 to 24, 2012 at MSRI, Berkeley, CA USA

The food provided during the workshop



| | | |
|-----------------------|----|-----|
| 1 -Not satisfactory | 1 | 2% |
| 2 | 6 | 11% |
| 3 | 12 | 22% |
| 4 | 17 | 31% |
| 5 -Above satisfactory | 18 | 33% |

Additional comments on the venue

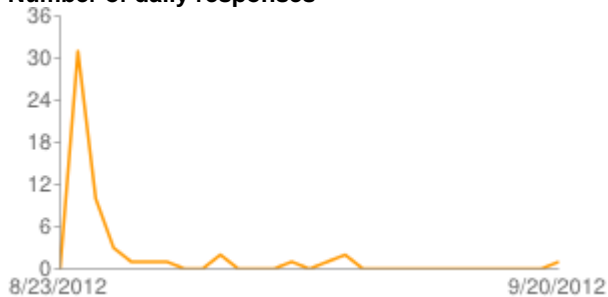
I hope workshops in future will provide more kinds of food. wow!
 what a view in every direction! I believe the food offerings should be more considerate of participants dietary restrictions and pref ...

Thank you for completing this survey

We welcome any additional comments or suggestions you may have to improve the overall experience for future participants.

It was great experience and I did enjoy this workshop a lot. Thank you for everything. The only reason I felt the poster session was not beneficial was that there were so few posters and too many people. It would have been better if more people were presenting posters. It would have spread the attendees out and given us a chance to visit with the presenters. Overall, I've had a very positive experience at MSRI. This is my first time here, and I would definitely like to attend an MSRI workshop again.

Number of daily responses



Connections for Women: Joint Workshop on Commutative Algebra and Cluster Algebras

August 22 to August 24, 2012

Additional Survey Responses

Additional comments on the topic presentation and organization

- It is wonderful
- the second talk on the first day was more of a research talk than an introductory talk
- With the exception of the minicourse the talks were extremely specialized. Perhaps speakers should be asked to give more of a colloquium-style talk in the future, especially when a diverse audience is expected.
- I am very happy to say I never expected such an incredible experience getting to meet so many wonderful people from staff to students to mathematicians. Thank you.
- Cluster talks were much more appropriate for a broad audience (I'm a commutative algebraist, and got more from the cluster talks).
- A few of the speakers assumed a bit too much on the part of the audience, particularly in view of the fact that people were coming from two rather different backgrounds. Several other speakers (from both camps) did spectacularly well in selling the subject and making it accessible to the "other camp".
- The mini course together with the exercise session were excellent.
- There was a good attempt to introduce cluster algebras, but the introductory lectures did not lead naturally to the lectures on Friday (although those lectures were very helpful for me personally).
- great to have a lot of time between lectures, to discuss
- Some of the research talks were too difficult
-

Additional comments on your personal assessment

- The lectures on Cluster Algebras were more accessible than the ones in Commutative Algebra. The latter were directed mainly to specialists, it seems; a pity.
- The talks really help me to understand more!
- As a commutative algebraist, I was ignorant of cluster algebras and cluster categories, but now I have some insight into how they relate to several aspects of my own work.
- The talks on Cluster Algebras were generally very accessible and enjoyable (especially Lauren Williams's minicourse). I had a really hard time with the commutative algebra research talks. Why so elementary with cluster algebras and so advanced with commutative algebra?
- the panel discussion was great!!! I (a guy) got several insights in what it's like to be a female mathematician.

Additional comments on the venue

- I hope workshops in future will provide more kinds of food.
- wow! what a view in every direction!
- I believe the food offerings should be more considerate of participants dietary restrictions and preferences.
- Have some sugar-free food.
- New (ish) caterer is much much better than several years ago. The location is wonderful as always.

- Hard to beat!
- very beautiful!
- MSRI is a wonderful place. Food a bit pricy.
- The snacks provided by MSRI are great but the catering needs more variety.

What other subjects should be addressed in future panel discussions?

- Hold the panel discussion earlier - it stimulates discussion.
- Probably it's best just to let things flow freely. This worked here and it should work in the future.
- If it is important for faculty to know about non-academic jobs and those which are academic but not necessarily as a professor. By know about I mean being able to guide theirs students towards those directions.
- the panel discussion was great!!! I (a guy) got several insights in what it's like to be a female mathematician.
-

We welcome any additional comments or suggestions you may have to improve the overall experience for future participants.

- It was great experience and I did enjoy this workshop a lot. Thank you for everything.
- "The only reason I felt the poster session was not beneficial was that there were so few posters and too many people. It would have been better if more people were presenting posters. It would have spread the attendees out and given us a chance to visit with the presenters.

Overall, I've had a very positive experience at MSRI. This is my first time here, and I would definitely like to attend an MSRI workshop again."