

# Mandi A. Schaeffer Fry

“Real Life”: Assistant Prof, MSU Denver



MSRI: Postdoc, GRTA

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Research Area:

Groups

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Research Area:

Finite Groups

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Research Area:

Representations of Finite Groups

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Research Area:

Representations of Finite Groups  
**Characters**

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Research Area:

Representations of Finite Groups (of Lie Type)  
**Characters**

## More Specifically...

- Galois action on characters

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  - Navarro's Galois-McKay and related conjectures

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- Irreducible restrictions
- Degree bounds